

Measurement of the Absolute Branching Fraction of the Inclusive Semileptonic Λ_c^+ Decay

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Using a data sample of e^+e^- collisions corresponding to an integrated luminosity of 567 pb^{-1} collected at a center-of-mass energy of $\sqrt{s} = 4.6 \text{ GeV}$ with the BESIII detector, we measure the absolute branching fraction of the inclusive semileptonic Λ_c^+ decay with a double-tag method. We obtain $\mathcal{B}(\Lambda_c^+ \rightarrow Xe^+\nu_e) = (3.95 \pm 0.34 \pm 0.09)\%$, where the first uncertainty is statistical and the second systematic. Using the known Λ_c^+ lifetime and the charge-averaged semileptonic decay width of nonstrange charmed mesons (D^0 and D^+), we obtain the ratio of the inclusive semileptonic decay widths $\Gamma(\Lambda_c^+ \rightarrow Xe^+\nu_e)/\bar{\Gamma}(D \rightarrow Xe^+\nu_e) = 1.26 \pm 0.12$.

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Since the first observation of the Λ_c^+ baryon, the lightest baryon containing a charm quark, in 1979 [1], its hadronic decays have been studied extensively. However, information about semileptonic decays of the Λ_c^+ baryon is sparse [2–6]. The measurement of the branching fraction of $\Lambda_c^+ \rightarrow \Lambda l^+\nu_l$ ($l = e, \mu$) was first performed by the ARGUS collaboration [3] and then by the CLEO collaboration [4] before 1994. Recently, the BESIII collaboration measured the absolute branching fraction of $\Lambda_c^+ \rightarrow \Lambda e^+\nu_e$ and $\Lambda_c^+ \rightarrow \Lambda \mu^+\nu_\mu$ to be $(3.63 \pm 0.43)\%$ [5] and $(3.49 \pm 0.53)\%$ [6], respectively. A comparison of the exclusive semileptonic decay branching fraction $\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda e^+\nu_e)$ and the inclusive semileptonic decay branching fraction $\mathcal{B}(\Lambda_c^+ \rightarrow Xe^+\nu_e)$, where X refers to any possible particle system, will guide searches for new semileptonic decay modes. In addition, using the known Λ_c^+ lifetime, the semileptonic decay width $\Gamma(\Lambda_c^+ \rightarrow Xe^+\nu_e)$ can be determined. Comparing $\Gamma(\Lambda_c^+ \rightarrow Xe^+\nu_e)$ with the charge-averaged nonstrange D semileptonic decay width $\bar{\Gamma}(D \rightarrow Xe^+\nu_e)$, the ratio $[\Gamma(\Lambda_c^+ \rightarrow Xe^+\nu_e)/\bar{\Gamma}(D \rightarrow Xe^+\nu_e)]$ can be obtained. Current data give $\Gamma(\Lambda_c^+ \rightarrow Xe^+\nu_e)/\bar{\Gamma}(D \rightarrow Xe^+\nu_e) = 1.44 \pm 0.54$ [7,8]. This ratio is predicted to be 1.67 [8,9] using an effective-quark theory calculation and about 1.2 based on a calculation using the heavy-quark expansion [10]. Therefore, a more

precise measurement of $\mathcal{B}(\Lambda_c^+ \rightarrow Xe^+\nu_e)$ is desirable to test these theoretical predictions.

Measurement of $\mathcal{B}(\Lambda_c^+ \rightarrow Xe^+\nu_e)$ was only performed by the MARK II collaboration in 1982, with a result of $(4.5 \pm 1.7)\%$ [11] using an e^+e^- collision data sample taken at center-of-mass energies from 4.5 to 6.8 GeV. The determination of $\mathcal{B}(\Lambda_c^+ \rightarrow Xe^+\nu_e)$ is obtained from signal events containing $\bar{\Lambda}e^+(\bar{p}e^+)$ [12], with the observed $\bar{\Lambda}(\bar{p})$ serving as a tag for a charmed baryon event. All these events are assumed to be from charmed baryon pair production and subsequent Λ_c^+ semileptonic decay. This assumption should be questioned as there are $e^+e^- \rightarrow c\bar{c} \rightarrow \bar{D}\bar{p}\Lambda_c^+X$ continuum events [13]. Besides, they need to estimate the total number of produced charmed baryon events, which has large uncertainties and is model dependent [1]. In this Letter, we present the first absolute measurement of $\mathcal{B}(\Lambda_c^+ \rightarrow Xe^+\nu_e)$ by employing a double-tag technique [14]. This technique takes advantage of a clean $\Lambda_c^+\bar{\Lambda}_c^-$ sample just above the threshold and, thus, obviates the need to make the above assumption or estimate the total number of produced charmed baryon events.

Our measurement is performed by analyzing an e^+e^- collision data sample of 567 pb^{-1} accumulated at $\sqrt{s} = 4.6 \text{ GeV}$ and recorded with the BESIII detector [15] at the Beijing Electron-Positron Collider II (BEPCII) [16]. A detailed description of the BESIII detector can be found in Ref. [15].

A GEANT4-based [17] Monte Carlo (MC) simulation is used to estimate the signal efficiency, optimize the selection criteria, and understand the backgrounds. In the simulation, the effects of beam-energy spread and initial state radiation (ISR) are incorporated using KKMC [18], and the final-state

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radiation (FSR) is modeled by PHOTOS [19]. A MC sample consisting of $\Lambda_c^+ \bar{\Lambda}_c^-$ pairs, $D_{(s)}^{(*)} \bar{D}_{(s)}^{(*)}$ pairs, ISR to lower-mass charmonium (ψ) states, and continuum processes incorporates most expected channels. The known decay modes are modeled with EVTGEN [20,21] using branching fractions taken from the Particle Data Group (PDG) [7], and the remaining unknown decays from the charmonium states with LUNDCHARM [22].

A double-tag technique, first developed by the MARK III collaboration [23], is employed. First, we fully reconstruct one $\bar{\Lambda}_c^-$ and, then, search for candidates of the signal decay in the rest of the event that is recoiling against the tagged $\bar{\Lambda}_c^-$. Hence, the absolute branching fraction of the inclusive semileptonic decay can be measured without knowing the total number of $\Lambda_c^+ \bar{\Lambda}_c^-$ pairs produced, thus, eliminating the related systematic uncertainty. The tag candidates are reconstructed through the decays $\bar{\Lambda}_c^- \rightarrow \bar{p} K_S^0$ and $\bar{\Lambda}_c^- \rightarrow \bar{p} K^+ \pi^-$, which have large branching fractions and low backgrounds.

The charged tracks, except those from K_S^0 , are required to have a polar angle θ with respect to the beam direction within the multilayer drift chamber (MDC) acceptance $|\cos\theta| < 0.93$, and a distance of closest approach to the interaction point (IP) within 10 cm along the beam direction and 1 cm in the plane transverse to the beam direction. Particle identification (PID) for charged pions, kaons, and protons is performed by exploiting time-of-flight (TOF) information and specific ionization energy loss dE/dx measured by the MDC. The confidence level (C.L.) under each particle hypothesis (p , K , or π) is calculated; each charged track is assigned the particle type with the largest PID C.L. The K_S^0 meson candidates are reconstructed from two oppositely charged tracks to which no PID criteria are applied and which are assigned the pion mass hypothesis. The charged tracks from the K_S^0 candidate must satisfy $|\cos\theta| < 0.93$. Furthermore, due to the long lifetime of the K_S^0 meson, there is a less stringent criterion on the distance of closest approach to the IP in the beam direction of less than 20 cm, and there is no requirement on the distance of closest approach in the plane transverse to the beam direction. The invariant mass of the track pair is required to be in the range $(0.487, 0.511)$ GeV/c^2 . Furthermore, the $\pi^+ \pi^-$ pair is constrained to be consistent with originating from a common decay vertex by means of a vertex fit. In addition, the decay length, which is the distance between the IP and the decay vertex, is required to be larger than twice its resolution.

To suppress combinatorial backgrounds, two kinematic variables are used to select the tag candidates. These are the energy difference $\Delta E \equiv E_{\bar{\Lambda}_c^-} - E_{\text{beam}}$ and the beam-constrained (BC) mass $M_{\text{BC}} \equiv \sqrt{E_{\text{beam}}^2/c^4 - |\vec{p}_{\bar{\Lambda}_c^-}|^2/c^2}$, where E_{beam} is the beam energy, $E_{\bar{\Lambda}_c^-}$ and $\vec{p}_{\bar{\Lambda}_c^-}$ are the reconstructed energy and three momentum of the tag

TABLE I. Summary of ΔE requirements, detection efficiencies, and tag yields for the different tag modes.

Tag mode	ΔE (MeV)	Efficiency (%)	Yield
$\bar{\Lambda}_c^- \rightarrow \bar{p} K_S^0$	(-21, 19)	56.5 ± 0.3	1214 ± 36
$\bar{\Lambda}_c^- \rightarrow \bar{p} K^+ \pi^-$	(-20, 16)	50.1 ± 0.1	6092 ± 82

candidate in the rest frame of the $e^+ e^-$ system, respectively. We require ΔE to be within $(-3\sigma, 3\sigma)$ of the peak of the ΔE distribution, where σ is the resolution of the ΔE distribution. Table I gives the ΔE requirements for each tag mode. If there are multiple candidates for the same tag mode in a given event, only the combination with the smallest $|\Delta E|$ is retained for further analysis. To determine the tag yields, we apply a fit to the M_{BC} distributions, as shown in Fig. 1. In the fits, the signal shape is modeled by the shape derived from MC simulation convolved with a Gaussian function that describes the resolution difference between data and MC simulation; the combinatorial background is described by an ARGUS function [24]. We obtain the tag yields by subtracting the integral of the background function in the signal region $2.282 < M_{\text{BC}} < 2.300$ GeV/c^2 from the total number of events in the same region. The tails of the M_{BC} distribution above the nominal Λ_c^+ mass are due to the effects of ISR and FSR. The tag yields and the corresponding detection efficiencies are summarized in Table I.

In the selected tag sample of $\bar{\Lambda}_c^-$ candidates, we search for charged tracks consistent with being an electron or positron. To ensure that the charged tracks originate from the IP, the same distance of closest approach selection criteria are used as for the non- K_S^0 daughters of the tag candidates. The track is required to satisfy $|\cos\theta| < 0.8$ to ensure that it lies within the acceptance of the barrel of the electromagnetic calorimeter (EMC), which has better energy resolution than the EMC end caps. The momentum of the charged track is required to be greater than 200 MeV/c , as it is difficult to separate positrons from other particles with low momenta. The selected tracks are divided into right-sign and wrong-sign samples, where the

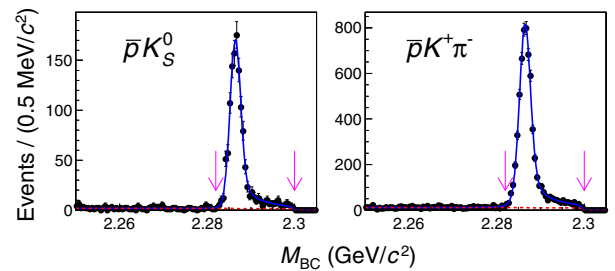


FIG. 1. M_{BC} distributions for the different tag modes in data. The solid blue line is the total fit, the dashed red line is the background component, and the pink arrows denote the M_{BC} signal region.

charge of the right-sign (wrong-sign) track is required to be opposite (equal) to that of the tag candidate.

The PID of the selected tracks is implemented with the information of the dE/dx , TOF and EMC, and the C.L. under each particle hypothesis (e , π , K , or p) is calculated. Positron candidates must satisfy $C.L.(e) > 0.001$ and $C.L.(e)/[C.L.(e) + C.L.(\pi) + C.L.(K) + C.L.(p)] > 0.8$. To further suppress the backgrounds from charged pions, $E_e/p_e > 0.8$ is required, where E_e and p_e are the deposited energy in the EMC and momentum measured by the MDC, respectively. The remaining selected charged tracks are assigned the hadron type corresponding to the highest C.L. that is greater than 0.001. The track is rejected if it does not have a C.L. greater than 0.001 for any hypothesis.

The identified positron sample contains sizable backgrounds from misidentified hadrons. To evaluate these backgrounds, knowledge of their yields and corresponding misidentification probabilities is required. The real right-sign and wrong-sign positron yields are determined individually by unfolding the matrix [25–27]

$$\begin{pmatrix} N_e^{\text{obs}} \\ N_\pi^{\text{obs}} \\ N_K^{\text{obs}} \\ N_p^{\text{obs}} \end{pmatrix} = \begin{pmatrix} P_{e \rightarrow e} & P_{\pi \rightarrow e} & P_{K \rightarrow e} & P_{p \rightarrow e} \\ P_{e \rightarrow \pi} & P_{\pi \rightarrow \pi} & P_{K \rightarrow \pi} & P_{p \rightarrow \pi} \\ P_{e \rightarrow K} & P_{\pi \rightarrow K} & P_{K \rightarrow K} & P_{p \rightarrow K} \\ P_{e \rightarrow p} & P_{\pi \rightarrow p} & P_{K \rightarrow p} & P_{p \rightarrow p} \end{pmatrix} \begin{pmatrix} N_e^{\text{true}} \\ N_\pi^{\text{true}} \\ N_K^{\text{true}} \\ N_p^{\text{true}} \end{pmatrix},$$

where N_a^{obs} is the observed yield of particle species a (a denotes e , π , K , or p), $P_{a \rightarrow b}$ is the probability of identifying particle a as particle b , and N_a^{true} is the true yield of particle a in the studied sample. The elements of the PID efficiency matrix $P_{a \rightarrow b}$ are obtained by studying corresponding control samples selected from data. The charged pion and proton samples are selected from $J/\psi \rightarrow p\bar{p}\pi^+\pi^-$ events. The charged kaon and positron samples are selected from $J/\psi \rightarrow K^+K^-K^+K^-$ and radiative Bhabha events, respectively. Because of the different event topologies, the PID efficiency of positrons from $\Lambda_c^+\bar{\Lambda}_c^-$ pairs (one positron and several hadrons) differs from that from radiative Bhabha scattering events (one electron, one positron, and one shower). The relative difference ($\sim 4.2\%$) is corrected by comparing the positron efficiency obtained from radiative Bhabha MC samples and $\Lambda_c^+\bar{\Lambda}_c^-$ pair MC samples. No correction to the other elements is implemented. The momentum dependence of the PID efficiency matrix is mostly determined in intervals of 100 MeV/ c , though some intervals are wider due to limited statistics, as presented in Fig. 2. The muon component is omitted in the unfolding procedure due to its small yields (almost the same as the positron yields), the small mis-PID probability from muon to positron (similar to that from pion to positron, shown in Fig. 2) and the negligible effect on the branching fraction measurement. In addition, because the selected pion sample contains the muon component

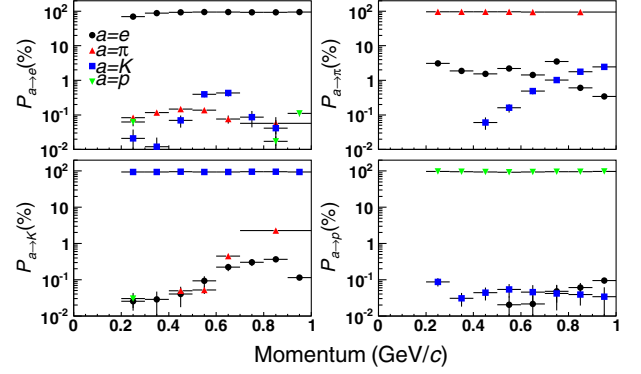


FIG. 2. PID efficiencies obtained from data.

due to their similar PID behavior in the BESIII detector, the muon component is implicitly taken into account.

To estimate the contribution from non- Λ_c^+ decays in the signal region, the unfolded positron yield in the M_{BC} sideband region is scaled by a factor of 0.78 that accounts for the relative amount of background in the sideband and signal regions determined by the fit to the M_{BC} distribution. Since low-background tag modes are used, the contribution from non- Λ_c^+ decays is small (3.8%).

The right-sign sample contains primary positrons, which directly originate from Λ_c^+ decays, and secondary positrons, not directly arising from Λ_c^+ decays and originating predominantly from γ conversions and π^0 Dalitz decays. Detailed MC studies indicate that the secondary positrons are charge symmetric; hence, their yield can be evaluated from the wrong-sign positron sample and subtracted from the total right-sign positron yields. The reliability of the wrong-sign subtraction has been validated by MC studies.

The tracking efficiency in a given momentum interval, including geometrical acceptance (80% due to the cut of $|\cos\theta| < 0.8$), track reconstruction efficiency, selection efficiency, and resolution effects, is corrected by unfolding the following matrix equation:

$$N_i^{\text{true}} = \sum_j T(i|j)N_j^{\text{pro}}, \quad (1)$$

where the tracking efficiency matrix $T(i|j)$ describes the probability of positrons produced in the j th momentum interval to be reconstructed in the i th momentum interval, N_j^{pro} is the number of primary positrons produced in the j th momentum interval, and N_i^{true} is the true yield of positron reconstructed in the i th momentum interval. The tracking efficiency matrix is obtained by studying the positron MC sample selected from Λ_c^+ semileptonic events. After this procedure is applied, we obtain the efficiency-corrected positron momentum spectrum above 200 MeV/ c in the laboratory frame. Table II summarizes the positron yields obtained after each correction step.

The fraction of positrons below 200 MeV/ c is obtained by fitting the efficiency-corrected positron momentum

TABLE II. Positron yields in data after each procedure. The uncertainties are statistical.

$\Lambda_c^+ \rightarrow Xe^+\nu_e$	Right sign	Wrong sign
Observed yields		
Tag signal region	228.0 ± 15.1	26.0 ± 5.1
Tag sideband region	11.0 ± 3.3	2.0 ± 1.4
PID unfolding		
Tag signal region	250.1 ± 17.1	28.3 ± 6.2
Tag sideband region	12.1 ± 3.8	1.7 ± 1.5
Sideband subtraction	240.7 ± 17.4	27.0 ± 6.3
Wrong-sign subtraction	213.7 ± 18.5	
Correction of tracking efficiency	272.1 ± 23.5	

spectrum with the sum of the spectra of the exclusive decay channels (Table III), as shown in Fig. 3. In the fit, the branching fraction of each component is allowed to vary within the given uncertainty. From the fit, we obtain the fraction of positrons below 200 MeV/c to be $(5.6 \pm 1.5)\%$, where the uncertainty is systematic derived from variations of the fit assumptions. The branching fraction of the inclusive semileptonic decay of the Λ_c^+ baryon is then calculated with

$$\mathcal{B}(\Lambda_c^+ \rightarrow Xe^+\nu_e) = \frac{N^{\text{pro}}(p_e > 200 \text{ MeV}/c)}{N_{\text{tag}}[1 - f(p_e < 200 \text{ MeV}/c)]}, \quad (2)$$

where $N^{\text{pro}}(p_e > 200 \text{ MeV}/c)$ is the yield of positrons with momentum p_e above 200 MeV/c after the correction of the tracking efficiency, N_{tag} is the tag yield, and $f(p_e < 200 \text{ MeV}/c)$ is the fraction of positrons below 200 MeV/c. Finally, we obtain $\mathcal{B}(\Lambda_c^+ \rightarrow Xe^+\nu_e) = (3.95 \pm 0.34)\%$, where the uncertainty is statistical only.

The systematic uncertainties in this analysis are listed in Table IV. The tag yield systematic uncertainty is estimated to be 1.0% by using alternative fits to the M_{BC} distribution with different signal shapes, background parameters, and fitting ranges. The systematic uncertainty related to

TABLE III. Λ_c^+ semileptonic decays used to extrapolate the positron momentum spectrum. The branching fraction of the $\Lambda_c^+ \rightarrow \Lambda e^+\nu_e$ decay is from the BESIII measurement [5] and the uncertainty of the unobserved decay channels is 100% of the predicted branching fractions. The form factor of the $\Lambda_c^+ \rightarrow \Lambda e^+\nu_e$ decay is taken from QCD sum rules [28] and the other two, unobserved, semileptonic decay modes are generated by PYTHIA [29] according to the simple $V - A$ matrix element.

Decay channel	\mathcal{B} (%)	Model
$\Lambda_c^+ \rightarrow \Lambda e^+\nu_e$	3.63 ± 0.43 [5]	$F_1^V(q^2)$ $= 2.52/5.09 - q^2$ [28]
$\Lambda_c^+ \rightarrow \Lambda(1405)e^+\nu_e$	0.38 ± 0.38 [30]	PYTHIA [29]
$\Lambda_c^+ \rightarrow ne^+\nu_e$	0.27 ± 0.27 [31]	PYTHIA [29]

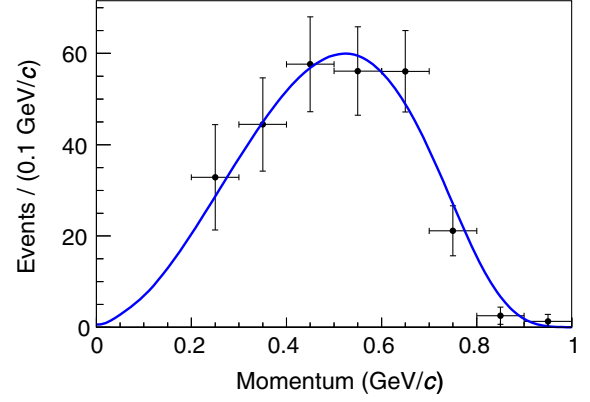


FIG. 3. Extrapolation of the positron momentum spectrum in the laboratory frame obtained from data, shown as points with error bars. The blue curve shows the extrapolated spectrum.

the tracking efficiency is estimated to be 1.0% by studying radiative Bhabha scattering events [5]. The systematic uncertainty in the positron identification efficiency is estimated by comparing the positron PID efficiencies in different MC simulated semileptonic Λ_c^+ decays. The largest relative difference of the positron PID efficiency is assigned as the systematic uncertainty. The uncertainties in the other elements of the PID efficiency matrix are estimated by comparing the matrix elements obtained from $\Lambda_c^+ \bar{\Lambda}_c^-$ pair MC samples with those obtained from MC samples of radiative Bhabha events, $J/\psi \rightarrow p \bar{p} \pi^+ \pi^-$ and $J/\psi \rightarrow K^+ K^- K^+ K^-$ MC samples. Adding them in quadrature, we assign 0.9% as the systematic uncertainty related to PID. The uncertainty associated with the M_{BC} sideband subtraction is estimated to be 0.5% by using an alternative M_{BC} sideband region. To estimate the uncertainty in the extrapolation of the positron momentum spectrum, we perform an alternative fit in which the branching fraction of each fit component is unconstrained. In addition, we use an alternative form-factor model and repeat the fit. Adding these effects in quadrature, we attribute 1.5% as the systematic uncertainty related to the extrapolation procedure. The uncertainty due to limited statistics of data and MC simulation used to determine the PID efficiency matrix and tracking efficiency matrix is estimated by repeating the PID unfolding procedure and correction of tracking

TABLE IV. Sources of systematic uncertainties.

Source	Relative uncertainty (%)
Tag yield	1.0
Tracking	1.0
PID	0.9
Sideband subtraction	0.5
Extrapolation	1.5
Data and MC statistics	0.4
Sum	2.3

TABLE V. Comparison of the branching fraction (in 10^{-2}) and ratio of the semileptonic decay width between experimental measurements and theoretical predictions.

Result	$\Lambda_c^+ \rightarrow X e^+ \nu_e$	$\frac{[\Gamma(\Lambda_c^+ \rightarrow X e^+ \nu_e)]}{\bar{\Gamma}(D \rightarrow X e^+ \nu_e)}$
BESIII	3.95 ± 0.35	1.26 ± 0.12
MARK II [11]	4.5 ± 1.7	1.44 ± 0.54
Effective-quark method [8,9]		1.67
Heavy-quark expansion [10]		1.2

efficiency. In each repetition, we vary each element of the PID efficiency matrix and tracking efficiency matrix within the corresponding error simultaneously. The corresponding systematic uncertainty is derived from 10 000 independent repetitions and is estimated to be 0.4%. Adding all uncertainties in quadrature, the total systematic uncertainty is determined to be 2.3%.

The absolute branching fraction of the inclusive semileptonic decays of the Λ_c^+ baryon is determined to be $\mathcal{B}(\Lambda_c^+ \rightarrow X e^+ \nu_e) = (3.95 \pm 0.34 \pm 0.09)\%$, where the first and second uncertainties are statistical and systematic, respectively. Compared with the branching fraction of $\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e$ measured by the BESIII collaboration [5], the ratio $[\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e)/\mathcal{B}(\Lambda_c^+ \rightarrow X e^+ \nu_e)]$ is determined to be $(91.9 \pm 12.5 \pm 5.4)\%$, where the systematic uncertainty related to the tracking efficiency of the positron cancels. Using the known Λ_c^+ lifetime [7], we obtain the semileptonic decay width $\Gamma(\Lambda_c^+ \rightarrow X e^+ \nu_e) = (1.98 \pm 0.18) \times 10^{11} \text{ s}^{-1}$. Comparing this with the charge-averaged semileptonic decay width of nonstrange charmed mesons $\bar{\Gamma}(D \rightarrow X e^+ \nu_e)$ [7], the ratio $[\Gamma(\Lambda_c^+ \rightarrow X e^+ \nu_e)/\bar{\Gamma}(D \rightarrow X e^+ \nu_e)]$ is determined to be 1.26 ± 0.12 . A comparison of the branching fraction and ratio of the semileptonic decay width between experimental measurements and theoretical predictions can be found in Table V.

In summary, by analyzing a data sample corresponding to an integrated luminosity of 567 pb^{-1} taken at a center-of-mass energy $\sqrt{s} = 4.6 \text{ GeV}$, we report the absolute measurement of the inclusive semileptonic Λ_c^+ decay branching fraction $\mathcal{B}(\Lambda_c^+ \rightarrow X e^+ \nu_e) = (3.95 \pm 0.34 \pm 0.09)\%$. The uncertainty is reduced by a factor of 4 compared to the MARK II result [11]. Based on the BESIII measurements [5], we obtain the ratio of the branching fraction to be $[\mathcal{B}(\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e)/\mathcal{B}(\Lambda_c^+ \rightarrow X e^+ \nu_e)] = (91.9 \pm 12.5 \pm 5.4)\%$. We also determine the ratio $[\Gamma(\Lambda_c^+ \rightarrow X e^+ \nu_e)/\bar{\Gamma}(D \rightarrow X e^+ \nu_e)] = 1.26 \pm 0.12$, which restricts different models as given in Table V.

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- [1] G. S. Abrams *et al.* (MARK II Collaboration), *Phys. Rev. Lett.* **44**, 10 (1980).
- [2] M. Gronau and J. L. Rosner, *Phys. Rev. D* **97**, 116015 (2018).
- [3] H. Albrecht *et al.* (ARGUS Collaboration), *Phys. Lett. B* **269**, 234 (1991).

- [4] T. Bergfeld *et al.* (CLEO Collaboration), *Phys. Lett. B* **323**, 219 (1994).
- [5] M. Ablikim *et al.* (BESIII Collaboration), *Phys. Rev. Lett.* **115**, 221805 (2015).
- [6] M. Ablikim *et al.* (BESIII Collaboration), *Phys. Lett. B* **767**, 42 (2017).
- [7] C. Patrignani *et al.* (Particle Data Group), *Chin. Phys. C* **40**, 100001 (2016).
- [8] M. Gronau and J. L. Rosner, *Phys. Rev. D* **83**, 034025 (2011).
- [9] J. L. Rosner, *Phys. Rev. D* **86**, 014017 (2012).
- [10] A. V. Manohar and M. B. Wise, *Phys. Rev. D* **49**, 1310 (1994).
- [11] E. Vella *et al.* (MARK II Collaboration), *Phys. Rev. Lett.* **48**, 1515 (1982).
- [12] In MARK II measurement, events containing a p and not a \bar{p} are excluded to reduce the background from beam-gas interactions.
- [13] D. E. Jaffe *et al.* (CLEO Collaboration), *Phys. Rev. D* **62**, 072005 (2000).
- [14] Throughout this Letter, charge-conjugate modes are implied unless otherwise stated.
- [15] M. Ablikim *et al.* (BESIII Collaboration), *Nucl. Instrum. Methods Phys. Res., Sect. A* **614**, 345 (2010).
- [16] C. H. Yu *et al.*, *Proceedings of the IPAC2016, Busan, Korea, 2016* (JACoW, Geneva, 2016).
- [17] S. Agostinelli *et al.* (GEANT4 Collaboration), *Nucl. Instrum. Methods Phys. Res., Sect. A* **506**, 250 (2003).
- [18] S. Jadach, B. F. L. Ward, and Z. Wař, *Phys. Rev. D* **63**, 113009 (2001).
- [19] E. Richter-Was, *Phys. Lett. B* **303**, 163 (1993).
- [20] R. G. Ping, *Chin. Phys. C* **32**, 599 (2008).
- [21] D. J. Lange, *Nucl. Instrum. Methods Phys. Res., Sect. A* **462**, 152 (2001).
- [22] J. C. Chen, G. S. Huang, X. R. Qi, D. H. Zhang, and Y. S. Zhu, *Phys. Rev. D* **62**, 034003 (2000).
- [23] R. M. Baltrusaitis *et al.* (MARK III Collaboration), *Phys. Rev. Lett.* **56**, 2140 (1986).
- [24] H. Albrecht *et al.* (ARGUS Collaboration), *Phys. Lett. B* **241**, 278 (1990).
- [25] A. Hocker and V. Kartvelishvili, *Nucl. Instrum. Methods Phys. Res., Sect. A* **372**, 469 (1996).
- [26] N. E. Adam *et al.* (CLEO Collaboration), *Phys. Rev. Lett.* **97**, 251801 (2006).
- [27] D. M. Asner *et al.* (CLEO Collaboration), *Phys. Rev. D* **81**, 052007 (2010).
- [28] R. S. Marques de Carvalho, F. S. Navarra, M. Nielsen, E. Ferreira, and H. G. Dosch, *Phys. Rev. D* **60**, 034009 (1999).
- [29] T. Sjostrand, P. Edén, C. Friberg, L. Lönnblad, G. Miu, S. Mrenna, and E. Norrbin, *Comput. Phys. Commun.* **135**, 238 (2001).
- [30] M. Pervin, W. Roberts, and S. Capstick, *Phys. Rev. C* **72**, 035201 (2005).
- [31] M. A. Ivanov, V. E. Lyubovitskij, J. G. Körner, and P. Kroll, *Phys. Rev. D* **56**, 348 (1997).